

## A REVIEW OF GRAPH TOPOLOGICAL ANALYSES IN LOCATION-BASED SOCIAL NETWORKS

**Buse Saricayir**

[busesaricayir@gmail.com](mailto:busesaricayir@gmail.com)

Master's student of the "Computer Engineering"

Karabuk University, Karabuk, Turkiye

Scientific supervisor – **Caner Ozcan, Ismail Rakip Karas.**

### **Abstract**

The advent of location-based social networks (LBSNs) has fundamentally altered the manner in which social interaction occurs, integrating social interaction with a geographic location. This paper analyses the importance of graph topologies, with a particular focus on LBSNs, and the role of LBSN data. It draws upon 17 studies conducted between 2019 and 2024. All of the papers mentioned are part of the group using diagrammatic structures, but their gendering of the analysis to diagrammatic topology is not relevant. In contrast, they employ graph algorithms and structures to address issues pertaining to the construction of recommendation systems, the dissemination of information, and the safeguarding of information privacy. These papers are classified according to the appropriate use of graph structures for heterogeneous graphs, spatial network information/influence graphs and LBSN applications that are not primarily topology networks. This review illustrates the growing significance of graph techniques in LBSN-driven studies, while simultaneously highlighting a crucial gap: an insufficient examination of the topological characteristics of these networks and their impact on the performance and usability of applications.

**Keywords:** LBSN, Graph Topology, Graph, Location-based social network

### **Introduction**

Location-based social networks (LBSNs) have dramatically changed the environment since they allow users to combine geographical aspects with social networks and data sharing [1]. There

is the enhancement of check-ins, recommendations, geo-tagged content and location sharing, all done through the users' spatial information in these networks creating social context [2]. The immense growth that has come about with mobile technologies and advanced positioning systems greatly simplified and increased the complexity of these networks systems. All LBSNs have a graph topology structure, which acts as the basic architectural component, and defines the concepts of users, places and social networks. Graph topology is vital for spatial social understanding and such as the structure of a network, the interaction of users, information flow and spatial aspects of society [3]. There is a shift in resources from traditional methods of network analysis to more advanced graph theoretical approaches to unravel the structures that promote location-based interactions among members of a social network [4]. Moreover, this helped LBSN graph topologies grow even more due to the recent technological developments in machine learning, massive amounts of data, and geo-information. These developments have enabled more nuanced investigations into user behavior, community formation, and spatial-temporal patterns within social networks [5]. The intersection of graph theory, social network analysis, and location-based technologies has opened unprecedented avenues for understanding complex social phenomena [6]. The concept of LBSN is shown in Fig 1.

Methodologically, contemporary LBSN research has embraced interdisciplinary approaches, integrating perspectives from social network analysis, complex systems theory, geographical information science, and computational sociology. These multidisciplinary researches have revealed sophisticated insights into urban dynamics, social network structures, and human interaction patterns across different spatial and temporal scales [8]. Graph topology becomes a critical lens through which researchers can examine and model the complex, non-linear relationships inherent in location-based social interactions.

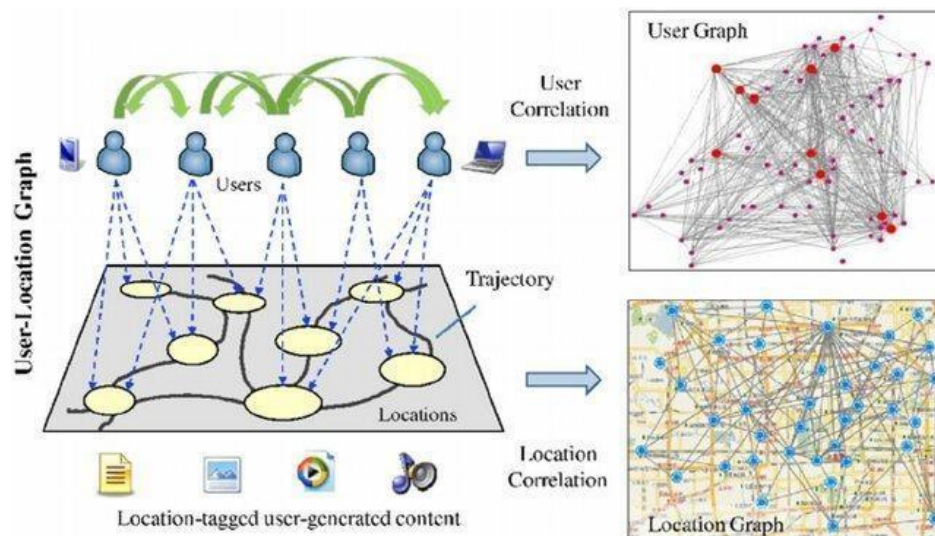


Figure 1 – Concept of location-based social networks [7]

Privacy and ethical considerations have simultaneously emerged as crucial research domains within LBSN studies. As location data becomes increasingly granular and personal, researchers and practitioners must navigate complex ethical landscapes, balancing technological innovation with individual privacy protection. Graph topology research has consequently evolved to incorporate privacy-preserving techniques, anonymization strategies, and robust data governance frameworks [9].

In this review, we will examine more closely the relationship between the topology of graphs and location-based networks, stating the benefits and identifying current tendencies and future perspectives. The purpose of this review is to synthesize findings from several publications and examples of social network analysis that substantiate the applicability of graph theory to the

representation of social relationships in localized environments, allowing for the discovery of new solutions.

### Related Works

In this study, all the papers analyzed use graph representations to depict LBSNs. However, the central focus of these papers is not on a thorough analysis of the graph topology. Rather, they primarily engage with the application of graph algorithms and structures to solve particular practical challenges related to LBSNs. This emphasis makes it difficult to categorize the papers strictly according to traditional graph topology classifications, such as small-world or scale-free networks. Therefore, we advocate for a classification method that groups the papers based on the various graph structures they incorporate. Table 1 presents a list of the studies that were reviewed in this paper.

Thereafter, we would identify and discuss all the topological considerations in the study, providing a clearer picture in relation to all of the diverse approaches in this body of literature. This allows a nuanced receipt of how different graph structures add up to the understanding and functioning of LBSNs in different contexts. In fact, Liu et al. have studied the information propagation in LBSNs in a very significant way in 2019 [10]. They understand information propagation by employing a graph structure in terms of the way in which the network is organized, with respect to the spreading of information. This research is mainly based on understanding the dynamics in which the information propagates and has not discussed much of the actual structure of the network. This points to the need for some more work in terms of these properties and organization's study under networks.

Other studies also use LBSN data and graph form for unrelated applications, and not necessarily focusing on topological analysis. For example, Diaz et al. [11] use a graph structure to contextualize the language modeling task. According to a clear view of the network but not probing into its bottom topologies, Sun et al. [12] investigated mechanisms that protect personal privacy, again working within a graph representation of the network but without any in-depth analysis of the network's structure. Also, Kim et al. [13] develop synthetic LBSN data, and Shen et al. [14] are on using LBSN data to personalize smart tourism applications. These studies demonstrate the expanding scope of applicability on graph representation in quite a lot of LBSN research without paying any attention to the details of the network topology.

Table 1 – Related works

Reference	Year	Graph Type	Topological Properties
Liu Et Al. [10]	2019	Implicit Spatial Network	Information Propagation Dynamics
Diaz Et Al. [11]	2022	Graph-Based Context For Language Modeling	None Explicitly Stated
Sun Et Al. [12]	2019	Graph Representation Of Lbsn	None Explicitly Stated
Kim Et Al. [13]	2020	Synthetic Lbsn Data Generation	Patterns Of Life (Implicit)
Shen Et Al. [14]	2024	Graph Representation For Personalized Tourism	None Explicitly Stated
Wang Et Al. [15]	2019	Heterogeneous Graph	Implicitly Uses Relationships Between Users And Pois
Qiao Et Al. [16]	2020	Heterogeneous Graph	Implicitly Uses Relationships Between Users And Pois
Yang Et Al. [17]	2020	Heterogeneous Hypergraph	Implicitly Captures Complex Relationships

Fei Et Al. [18]	2024	Heterogeneous Network	None Explicitly Stated
Yue-Qiang Et Al. [19]	2019	Implicit Spatial Network (Transition Graph)	User Mobility, Geographical Proximity
Rahimi Et Al. [20]	2020	Implicit Spatial Network	User Behavior, Geographical Context
Khazaei & Alimohammadi [21]	2019	Implicit Spatial Network	Geographical Proximity, User Context
Guo Et Al. [22]	2019	Implicit Spatial Network	Location Perspective, Neighborhood Awareness
Canturk Et Al. [23]	2023	Graph-Based Approach With Trust	Trust Relationships Within The Network
Comito [24]	2020	Implicit Spatial Network	User Mobility Patterns
Hosseinpour Et Al. [25]	2019	Implicit Spatial Network	Socio-Spatial Influence
Acharya & Mohbey [26]	2024	Spatial Network	High-Order Spatial Connectivity

The following sections delve into specific categories of graph representations used in LBSN research, moving beyond the general observation that explicit topological analysis is not the primary focus. These categories, while not strictly adhering to classical graph topology classifications, provide a structured way to understand the diverse approaches employed in the literature.

### Heterogeneous Graphs

There are a substantial number of researchers who are interested in the application of heterogeneous graphs in their research that includes the integration of multiple node types (users' nodes and location nodes), and the analysis of bridging these nodes. As shown in Fig 2, the studies conducted by Wang et al. [15] and by Qiao et al. [16] highlight the application of heterogeneous graph embedding frameworks. These frameworks are particularly beneficial for enhancing representation learning, allowing for a more sophisticated understanding of the data structure. This method is beneficial for understanding the multi-faceted nature of the LBSN dataset, yet it does not formulate a specific evaluation of the resulting topological properties.

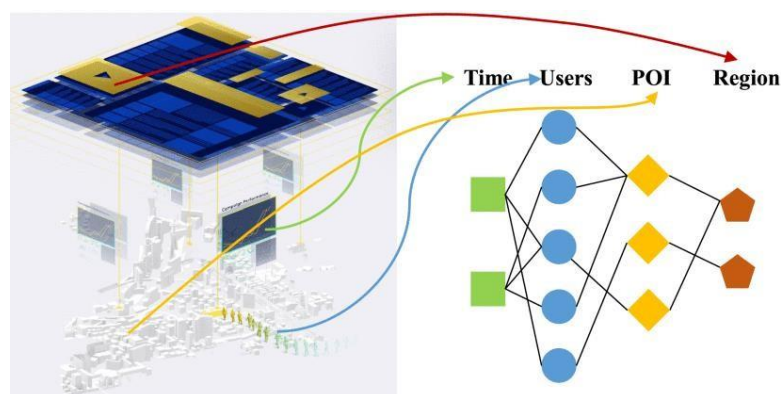


Figure 2 – Heterogeneous schema of LBSNs in the study conducted by Wang et al. [14].

Furthermore, Yang et al. [17] further extended this idea by extending their analysis to heterogeneous hypergraphs. This extension allows the capture of even more intricate and complex relationships between nodes, which is essential in the context of LBSNs. However, it still does not explicitly consider the topological structure of the hypergraph. Likewise, Fei et al. [18] also employed heterogeneous networks to estimate individual home locations, which demonstrated the

general applicability and feasibility of the method. Efforts of the sort acknowledge the complexity inherent to LBSNs, for which it is inappropriate to effectively treat graph models that are simple. However, such methods provide hints without taking an explicit design effort for a final topology resulting from these intertwined relationships.

### Spatial Networks

Many research articles implicitly depict spatial networks through their graph structures, illustrating the intricate relationships between various locations. For instance, studies that center on location recommendations, such as those conducted by Yue-Qiang et al. [19], Rahimi et al. [20], Khazaei and Alimohammadi [21], Guo et al. [22], and Canturk et al. [23], consistently take into account the factors of geographical proximity and user mobility patterns. These elements of user behavior and location interaction likely foster the phenomenon of spatial clustering, where certain locations become more favored by users based on their closeness and past visiting habits. Fig 3 illustrates an instance of a transition graph from one location to another.

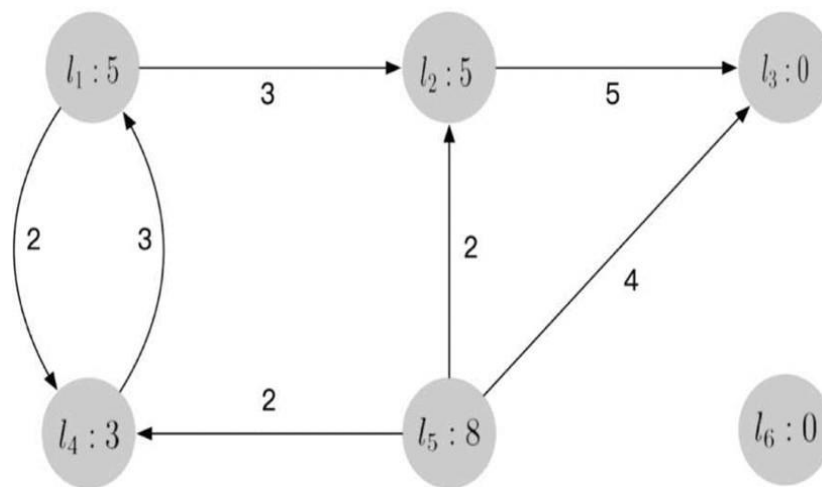


Figure 3 – An example of location-location transition graph from the study of Yue-Qiang et al. [19].

In a similar vein, the research presented by Comito [24] introduces a next-place prediction framework, which also recognizes the significance of spatial relationships inherent within the LBSN graph. Furthermore, the work done by Hosseinpour et al. [25], focusing on the maximization of socio-spatial influences, also indicates a reliance on the underlying spatial connections that characterize user interactions within this network. Additionally, Acharya & Mohbey [26] explicitly integrate spatial relationships into their recommendation framework through a method they describe as "high-order spatial connectivity mining". Although these studies utilize spatial information effectively, they typically do not focus on analyzing the specific topologies of the resulting spatial networks.

### Future Directions

Research that will be conducted in the future should emphasize the explicit characterization and analysis of the topologies of LBSN graphs. Degree distribution, clustering coefficients, path lengths, and community structure should all be explored by such properties. Understanding these properties will be the key to unlocking relevant insights into user behavior, information flow, and effectiveness of applications in LBSN domain. Moreover, research should start addressing the dynamic nature of graphs in LBSN, how these topological features will vary over time, or how they appear to be affected by external events. Such assessments on the temporal dimension will set the basis for LBSN applications which are adaptive and responsive over time. Finally, topological analysis can be abstracted to include other sources of data, such as user demographics or mobility patterns, to facilitate understanding on LBSN dynamics holistically, and to develop personalized, context-aware services. The research directions as indicated will therefore not only

advance theoretical knowledge concerning LBSNs, but will also step towards developing applications, which are more effective and user centric.

### **Conclusion**

This paper has demonstrated both the almost ubiquitous nature and the use of graph theoretic structures in the context of LBSN research. Although no of the papers under review set out primarily to study the topology of any graph, it is important to realize that the use of different graph algorithms and structural designs greatly enhance the quality of such research. Researchers across different fields of study often employ various forms of graph structures in solving particular problems and developing their contributions in LBSN. In order to grasp the scope of research activity in this field better, the classification of the articles based on the types of graph structures used is especially helpful. Concepts and structures of graphs and their applications in this case include heterogeneous graphs made up of nodes and edges representing various components and relationships, implicit spatial networks that depict the geographical context of location-based services, graphs representing information flow and how such information flows within a social network, and graphs evolved out of specific requirements in LBSN areas. This classification not only enables one to see how graph structures are employed and used in LBSN studies, but also emphasizes the range of approaches that scholars take. Each category corresponds to a particular view as to how graph theory could further clarification of social relatedness with regard to space – and only space – indicating the complex use of graph in this extremely active area of thinking.

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